Field of the Invention

The present invention relates to a method of spectrum analysis in two-dimensional representation to obtain accurate characteristic information on an object to be analyzed by using derivatives on spectral data of the said object in spectroscopic analysis.

Description of the Prior Art

spectroscopic analysis (including Heretofore, in infrared spectrophotometry and the like) in general, by measuring an intensity of light transmitting through the object to be analyzed (may hereafter be denoted as "analyzed object") characteristics various and converting absorbance, information in terms of physical and/or chemical properties (may hereafter be denoted as "characteristic information") including shapes, concentration, and the like of substances contained in the said analyzed object have been obtained based on the shapes of the said spectrum or a spectral profile. profile, that spectral spectral conventional representing absorbance of the analyzed object in terms of the wavenumber (or wavelength) are generally used (may hereafter be referred to as "absorbance/wavenumber spectral profile"). It can be considered that such a spectral profile is formed with a number of component bands overlapped.

As a means to analyze such spectral profiles, for example, the Japanese patent publication H11-148865 discloses the method of using derivatives on the spectral waveform of the analyzed object in spectroscopic analysis. To be concrete, as for the specific analyzed object, when spectral waveform where the intensity of the signal output of a spectrophotometer is represented as a function of wavenumber, wavelength, or time is prepared letting n1 and n2 (n1≠n2) be a positive integer, a method of spectrum analysis in two-dimensional representation with the following characteristics is disclosed. These characteristics are;

Calculating the n1-th and n2-th derivatives with respect to wavenumber, wavelength, or time of the said intensity of the signal output regarding the spectral profile on the said spectral data, plotting points on the two-dimensional coordinate plane whose X-coordinate is the said n1-th derivative the said n2-th derivative, and whose Y-coordinate is respectively, on the said two-dimensional coordinate plane, creating a two-dimensional plot of derivative pairs on the said spectral waveform, thereby obtaining specific information on the said spectral profile based on the two-dimensional plot of the said derivative pairs.

However, although the spectral analysis method cited in the Japanese patent publication H11-148865 can find component

bands when the spectral profile contains a (single) component band, it is difficult to find all these component bands and even to estimate them is extremely difficult when the spectral profile of the analyzed object contains several component bands overlapped. In particular, there are many cases that the spectral profile of the analyzed object has several overlapping component bands. Therefore, as for the analyzed object with a spectral profile containing several component bands, the method described in the Japanese patent publication H11-148865 can estimate the dominant component bands to some extent among the said component bands. However, as for unresolved bands buried under the dominant band, that is, the characteristics of those component bands are unclear due to severe overlap, it is extremely difficult even to estimate those bands.

SUMMARY OF THE INVENTION

Based on the method cited in the Japanese patent publication H11-148865, the present invention has been developed for further improvement. As a result of intensive studies, as for the specific analyzed object, when spectral data where the intensity of the signal output of a spectrophotometer is represented as a function of wavenumber, wavelength, or time, are prepared letting n and m $(n\neq m)$ be a positive integer, the inventor has proposed a method of spectrum analysis in two-dimensional representation for obtaining the specific

characteristic information on the said spectral data based on the said two-dimensional derivative plot by calculating the n-th and m-th derivatives with respect to wavenumber, wavelength, or time, of the said spectral data, plotting points on the two-dimensional coordinate plane as the X-Y coordinate system whose X-coordinate is the said n-th derivative and whose Y-coordinate is the said m-th derivative respectively on the said two-dimensional coordinate plane, and preparing the two-dimensional derivative plot on the said spectral data.

based on the characteristic information Further, described above, the inventor has proposed a method of spectrum analysis in two-dimensional representation which estimates the component bands comprising the spectral profile of the analyzed object by estimating band parameter values regarding at least one component band among the component bands contained in the spectral profile of the analyzed object, estimating at least one component band, obtaining the two-dimensional derivative plot with the specific remaining component bands removed by clearing the specific component band or specific component bands already estimated or the two-dimensional derivative plot from spectral profiles or the two-dimensional derivative plot of analyzed object, obtaining specific characteristic information based on the two-dimensional derivative plot of this specific component removed, estimating band parameter values on other component bands based on the said characteristic information,

and iterating the estimation of at least one of the other component bands thereby estimating component bands in order.

That is, the present invention is a method of estimating component bands in order, using a specific component band or specific component bands already estimated and estimating remaining component bands (including the ones not yet estimated, the ones desired to be optimal).

To be concrete, a preferred embodiment of the present invention, although not specifically limited, is, first of all, to estimate one component band BDi(i is a positive integer) by estimating the band parameter values for BDi among component bands contained in the spectral profile of the analyzed object based on the specific characteristic information on the spectral profile of the two-dimensional derivative plot.

Next, the preferred embodiment is to prepare the two-dimensional derivative plot with BDi removed, either creating the two-dimensional derivative plot with BDi removed by clearing the two-dimensional derivative plot of the component band BDj(j is a positive integer where $j \neq i$) from the two-dimensional derivative plot of the said analyzed object or obtaining the spectral profile with BDi removed by clearing a profile of BDi from a spectral profile of the said analyzed object.

Then, the preferred embodiment is to estimate one component band BDj by estimating band parameter values on BDj other than BDi among the component bands contained in the

spectral profile of the analyzed object based on the said characteristic information by obtaining the specific characteristic information based on the said two-dimensional derivative plot with BDi removed.

Next, the preferred embodiment is to prepare a two-dimensional derivative plot with BDj removed, either creating the two-dimensional derivative plot with at least BDj removed by clearing BDj or the two-dimensional derivative plot of both BDi and BDj from the two-dimensional derivative plot of the said analyzed object or obtaining the spectral profile with at least BDj removed by clearing BDj or the profile of both BDi and BDj from a spectral profile of the said analyzed object.

Then, the preferred embodiment is to estimate the component band BDk (k is a positive integer where at least k≠j) by estimating band parameter values on BDk other than BDj among the component bands contained in the spectral profile of the analyzed object based on the said characteristic information by obtaining the specific characteristic information based on the said two-dimensional derivative plot with BDi removed.

Thus, the present invention is a procedure of estimating other component bands in order as for component band contained in the spectral profile of the analyzed object, using the specific component band or specific component bands already estimated by iterating estimation of component bands, creating the two-dimensional derivative plot with information on an

estimated component band or estimated component band removed from the information on the analyzed object, acquiring the specific information based on this two-dimensional derivative plot and operating the estimation of other component bands based on this characteristic information.

In the two-dimensional derivative plot on spectral data of the analyzed object, the characteristic information on dominant component bands can be distinguished to some extent, however, as for characteristic information on unresolved component bands buried under the dominant component band, since it is subtle or since it overlaps with the characteristic information of other component bands overlapping with the said component band, the characteristic information of the said component band of its own becomes unclear and it is difficult to be distinguished.

Particularly, in the case where the overlapping component bands are dominant ones, the characteristic information on the unresolved component bands buried under the dominant component band can seldom be distinguished.

However, as the analytic method of the present invention shows, when the two-dimensional derivative plot is created by removing information on dominant component bands estimated from the characteristic information of the two-dimensional derivative plot of the analyzed object from the information about the analyzed object and by obtaining the two-dimensional

derivative plot based on the spectral profile after removal of information on dominant component bands, the characteristic information of component bands hidden by overlapping dominant component bands appears, which enables to obtain the characteristic information about component bands hidden by overlapping, and further enables to obtain the characteristic information which has never been achieved by the two-dimensional derivative plot on the spectral data of the analyzed object.

Then, by iterating the operations of removing the profile of single or several component bands already estimated from the information about the analyzed object and by obtaining the characteristic information using the two-dimensional derivative plot based on the removal thereafter estimating other component bands, estimating the component band contained in the spectral profile of the analyzed object in order with suitability can be achieved.

Thus, the method of estimating a single component band or several component bands contained in the spectral profile of the analyzed object and finding the other component bands in order by using the two-dimensional derivative plot obtained by removing the profile of the single component band or several component bands from the spectral profile of the analyzed object, or this procedure is called "Band Stripping".

Therefore, when the method of the present invention is employed, the component band that is contained in the spectral

profile of the analyzed object can be estimated easily.

Further, in the preferred embodiment of the present invention, the component band is a Gaussian band, a Lorentzian band, or the mixture thereof.

In the present invention, n is preferably 1 and/or 3 and m is n+1. When the combination of n and m is (n,m)=(1,2), (3,4), the characteristic information on the spectral data appears clearly. Therefore, when the two-dimensional derivative plot is created with the combination of (n,m)=(1,2) and/or (3,4), the characteristic information can be obtained easily.

According to the method of spectrum analysis in two-dimensional representation, in the two-dimensional derivative plot where pairs of the first and second derivatives are represented in the X-Y coordinate system, when a typical local minimum indicates the existence of a corresponding component band, an X position of the said local minimum is a first approximation of band center position Xc of the said component band, setting several points on the said two-dimensional derivative plot in the vicinity of Pa, point of intersection of the said two-dimenstional derivative plot with the X- axis, as candidates for the inflection point of the said component band, estimating the bandwidth of the said component band from the candidate of the said inflection point by the following Equation (1), estimating the peak height of the said component band from the distances between the said local minimum and the point(s)

of intersection of vertical line passing through the said local minimum and the horizontal line(s) passing through the said candidate points, obtaining the candidates for band parameter values of the said component band, and further obtaining the constraint conditions subjected to the band parameter values for the said component band from the said two dimensional derivative plot, the relation between the bandwidth bw and the X-position of the inflection point X_P of a single band can be preferably expressed by

$$b_w = (1/K_P) |X_C - X_P|$$
 (1)

(In Equation, b_W is an estimated value of the bandwidth of a Gaussian or a Lorentzian band, where the coefficient K_P is 0.42466 for Gaussian and 0.288675 for Lorentzian.)

According to the method of spectrum analysis in two-dimensional representation, in the two-dimensional derivative plot where pairs of the third and fourth derivatives are represented in the X-Y coordinate system, when a typical local maximum indicates the existence of a corresponding component band, an X position of the said local maximim is a first approximation of band center position Xc of the said component band, setting several points on the said two-dimensional derivative plot in the vicinity of Qd, point of intersection of the said two-dimenstional derivative plot with the X- axis, as candidates for the secondary inflection point of the said component

band from the candidate of the said secondary inflection point by the following Equation (2), estimating the peak height of the said component band from the distances between the said local maximim and the point(s) of intersection of vertical line passing through the said local maximum and the horizontal line(s) passing through the said candidate points, obtaining the candidates for band parameter values of the said component band, and further obtaining the constraint conditions subjected to the band parameter values for the said component band from the said two dimensional derivative plot, the relation between the bandwidth bw and the X-position of the secondary inflection point $X_{\mathbb{Q}}$ of a single band can be preferably expressed by

$$b_{W} = (1/K_{P}) |X_{C} - X_{Q}|$$
 (2)

(In the Equation, b_w is an estimated value of the bandwidth of a Gaussian or a Lorentzian band, where the coefficient K_Q is 0.31508 for Gaussian and 0.16426 for Lorentzian.)

In the present invention, the method of spectral analysis in two-dimensional representation which adjusts the already estimated band parameter values can preferably be used so that the specific component band already estimated and the complementary estimated component band with all the estimated component bands other than the said estimated specific component band removed from the spectral profile of the analyzed object or two-dimensional derivative plot coincide.

With the said band stripping method, the parameter values

of the each component band cannot be truly estimated and it sometimes fails into a so-called local optimum. This is because the adjacent component bands overlap and when the parameter values of the specific component band are too large or too small, the overestimation and/or underestimation affect(s) the parameter values such as band center position, bandwidth, and peak height of the adjacent component bands. Therefore, the present invention is capable of estimating the band parameter values for the component band with further suitability by introducing "complementary estimated component band".

The example of the coincidence between the specific estimated component band (denoted as eBD) and its complementary estimated component band (cBD) includes a method of minimizing the total sum of the distance of the iso-wavenumber lines between eBD and cBD in the two-dimensional derivative plots. By adjusting the parameter values for the specific estimated component band and by minimizing the difference between eBD and cBD, the estimated parameter values become as close to the true value as possible. In addition, by improving the degree of symmetry of the complementary estimated component band, the adjacent band parameter values are optimized. In other words, by adjusting the band parameter values for the specific estimated component band, the degree of symmetry of the complementary estimated component band is improved. Thus, introducing the complementary estimated component band and aiming to optimize

the estimated band parameter values already obtained is called "Complementary Matching" method.

The object of the present invention is to provide a method of spectrum analysis that can easily estimate its several component bands of the analyzed object having spectral profile containing several component bands. In addition, it can be applicable to spectral data such as infrared spectra, visible light spectra, ultraviolet spectra, Raman spectra, X-ray diffractogram, and chromatogram, and the like.

BRIEF DESCRIPTION OF THE DRAWINGS

Figure 1 is a graph depicting an original spectrum having three component bands overlapped.

Figure 2 is a graph depicting a second derivative spectrum of the original one shown in Fig.1.

Figure 3 is a graph depicting a fourth derivative spectrum of the original one shown in Fig.1.

Figure 4 is D1-D2 plots for OV3 and OV12.

Figure 5 is D3-D4 plots for OV3 and OV12.

Figure 6 is a graph showing the permissible range of the bandwidth and peak height for BD3 estimation.

Figure 7 is D1-D2 plots for OV12 and BD1.

Figure 8 is D1-D2 plots for OV13 and BD1.

Figure 9 is D1-D2 plots for OV13 and BD3.

Figure 10 is D1-D2 plots for OV12 and eOV12.

Figure 11 is a graph showing the permissible range of the

bandwidth and peak height for BD2 estimation.

Figure 12 is D1-D2 plots for eOV13.

Figure 13 is a graph showing the permissible range of the bandwidth and peak height for BD3 estimation.

Figure 14 is D1-D2 plots for BD1 and eBD1.

Figure 15 is a graph depicting spectral profile of eBD1, eBD2, eBD3, eOV3, and OV3.

Figure 16 is D1-D2 plots for eOV3 and OV3.

Figure 17 is D1-D2 plots for eBD3 and cBD3.

Figure 18 is D1-D2 plots for eBD 2 and cBD2.

Figure 19 is D1-D2 plots for eBD 1 and cBD1.

Figure 20 is D1-D2 plots for eBD 3 and cBD3 after the parameter values are improved by SumLS.

Figure 21 is D1-D2 plots for eBD 2 and cBD2 after the parameter values are improved by SumLS.

Figure 22 is D1-D2 plots for eBD 1 and cBD1 after the parameter values are improved by SumLS.

Figure 23 is D1-D2 plots for eBD 3 and cBD3 after the parameter values are improved in coincidence and symmetry.

Figure 24 is D1-D2 plots for eBD 2 and cBD2 after the parameter values are improved in coincidence and symmetry.

Figure 25 is D1-D2 plots for eBD1 and cBD1 after the parameter values are improved in coincidence and symmetry.

DESCRIPTION OF THE PREFERRED EMBODIMENT

The present invention is explained in detail based on the

drawings. Figure 1 shows the original spectrum generated (or synthesized) that is consisted of the three overlapping component bands. The explanation goes as for a method of estimating component band from these graphs.

As a shape of the component band estimated by the spectral analysis method of the present invention, a Gaussian band, a Lorentzian band, or a mixture thereof can be considered.

A Gaussian band is expressed by the following Equation:

BDG(X) = phg exp
$$\{-4 \log 2 (X-bcg)^2/bwg^2\}$$
 (3)

(in the Equation, bcg is the center position of the band, phg the peak height, and bwg2 the bandwidth.)

A Lorentzian band is expressed by the following Equation:

$$BD_L(X) = ph_L / \{1 + 4 (X-bc_L)^2/bw_L^2\}$$
 (4)

(in the Equation, bc_L is the center position of the band, ph_L the peak height, and bw_L the bandwidth.)

A mixture of a Gaussian and a Lorentzian band is expressed by the following Equation:

$$BD_{m}(X) = mBD_{G}(X) + (1-m)BD_{L}(X)$$
 (5)

(in the Equation, BDG(X) is the Gaussian band given by Equation (3), BDL(X) the Lorentzian band given by Equation (4), and m is the ratio of the mixture where 0 < m < 1.)

Further, the bandwidth is the full-width at half-height of the band (FWHH). In other words, the bandwidth is the distance between the two X positions at half-height of the band.

In the present invention, in order to find one component

band which is contained in the original spectrum, the characteristic information is so obtained as by differentiating the original spectrum. "n-th-m-th two-dimensional derivative spectral profile" is so defined as the one with the n-th derivative on the X-axis and the m-th derivative on the Y-axis. In some cases, it is abbreviated as "Dn-Dm plot".

Figure 1 shows the original spectrum of OV_3 (=BD1+BD2+BD3) having BD1, BD2, and BD3, three Gaussian component bands overlapped and spectral profile of each component band. That is, OV_3 is obtained by summing the component bands calculated by the following Equation (6).

$$BD_{i}(X) = ph_{i} exp \{-4 log 2 (X-bc_{i})^{2}/bw_{i}^{2}\}$$
 (6)

(in the Equation, i is 1, 2 or 3, representing the ith band, bcithe center position of the band, phi the peak height, and bwi the bandwidth.)

Spectral analysis is performed with Mathematica, mathematical software packages (ver. 2.2, Wolfram Research, Inc., IL). The band parameter values for the individual component band are given as follows:

Component band BD1: bc1 = -0.5978

 $bw_1 = 1.1070$

 $ph_1 = 0.6504$

Component band BD2: bc2 = 0.0012

 $Bw_2 = 0.9643$

 $ph_2 = 1.0630$

Component band BD3: bc3 = 0.4533

 $Bw_3 = 0.8078$

 $ph_3 = 0.8123$

In the simulation study estimating the component band, the parameter values are treated as unknown, however, the true parameter values described above are sometimes utilized in the course of the following explanation for evaluation of obtained results.

Mathematica is also used for calculations and drawings. In differential operation, analytic differentiation is performed and digitized with an interval of 0.01 so as to avoid the error caused by digital differentiation.

Here, in the usual spectral profile, the X-coordinate represents wavenumber, wavelength, or time, whereas the Y-coordinate represents absorbance. For convenience, the explanation goes defining that the X-coordinate represents wavenumber and the Y-coordinate represents absorbance. Further, the range of the X-coordinate is $-2 \le x \le 2$. Here, in this specification, "the n-th derivative spectrum" is denoted as the derivative spectrum with the quantity of the Y-axis differentiated the n-th with respect to the X-axis. In addition, "two-dimensional derivative plot" is denoted as the derivative plot with the n-th derivative on at least one axis of the two axes in the two-dimensional coordinate plane as the X-Y coordinate system.

In the analytical procedure of the method of this invention, first, a two-dimensional plot of the analyzing spectrum is created, and band parameter values for at least one component band within the two-dimensional plot are estimated after obtaining the characteristic information. For this purpose, the characteristics of the component band are explained as below. (Characteristic points of the component band)

In Fig. 1, among the three component bands, the characteristic points are shown as for the sharpest (with the narrowest bandwidth) component band BD3. Point T3 ($X_{T3}=0.4533$) is the vertex. (X_{T3} represents the X position of the point T3 and the same representation follows hereafter.) Points P31 ($X_{P31}=0.1103$) and P32 ($X_{P32}=0.7963$) are the zero-crossing points of the second derivative and the inflection points. Points Q32 ($X_{Q32}=0.1988$) and Q33 ($X_{Q33}=0.7078$) are the innermost zero-crossing points of the fourth derivative and the inflection points. Hereafter, the innermost zero-crossing points of the fourth derivative are called secondary inflection points.

In estimating the parameter values for component band BD3, band center position bc3 can be estimated by the corresponding local minimum or maximum, and bandwidth bw3 can be estimated by the following Equation. However, peak height ph3 cannot be estimated easily. When point B $_{\rm K}$ is so placed as the point where X=XT3 on OV12 which is obtained by removing BD3 from OV3, and when point T3' is so placed as the point where X= XT3 on OV3, the length

of line segment T_3 'Bk corresponds to peak height ph3. Therefore, if the X position of point Bk can be estimated, peak height ph3 can also be estimated.

Bandwidth bwi of component band BDi can be calculated from XPi1, the X position at inflection point Pi1, or from XPi2, the X position at inflection point Pi2, by the following Equations:

$$bwi = (1/K_P) |bci-x_{pi1}|$$
 (7)

$$bwi = (1/K_P) |b_{Ci}-x_{Pi2}|$$
 (8)

 $(K_P = 0.4247 \text{ in the case of a Gaussian band, whereas } K_P = 0.2887$ in the case of a Lorenztian band.)

Bandwidth bwi of component band BDi can be calculated from X_{Qi2} , the X position at the secondary inflection point Qi2, or from X_{Qi3} , the X position at secondary inflection point Qi3, by the following Equations:

$$bw_i = (1/K_Q) |b_{Ci}-x_{Qi1}|$$
 (9)

$$bwi = (1/K_0) |bci-x_{0i2}|$$
 (10)

 $(K_Q = 0.3151 \text{ in the case of a Gaussian band, whereas } K_Q = 0.1625$ in the case of a Lorenztian band.)

In order to estimate each component band, it is necessary to find a typical local minimum, local maximum, and the inflection points of the corresponding component band on OV3 where all component bands overlap. For this purpose, first, the feature of OV3 is studied by means of its derivative.

The second derivative spectrum of the original one in Fig. 1 is shown in Fig.2, while the fourth derivative spectrum in

Fig.1 is shown in Fig.3. OV_{12} is the spectrum where BD₃ is subtracted from OV_3 (i.e., $OV_{12} = OV_3 - BD_3$) or the spectrum where BD₁ and BD₂ overlap(i.e., $OV_{12} = BD_1 + BD_2$). In Fig.2, Min3 is the local minimum, points P_a and P_d are the inflection points of OV_3 .

Points P31' and P32' correspond to inflection points P31 and P32 of BD3 and they are the isosbestic points in the second derivative. As in the initial spectral profile, the length of line segment T3'BK corresponds to the peak height of BD3. It should be noted that a peak height of a differential spectrum does not equal that of an original spectrum, and it should be calculated based on a peak height at the second-order differentiation of a Gaussian band with a unit peak height (phi=1) having the same bandwidth.

In the fourth derivative in Fig.3, Max3 is the local maximum, and points Q_C and Q_d are the inflection points of the second derivative of OV3. Points Q_{32} ' and Q_{33} ' correspond to secondary inflection points Q_{32} and Q_{33} of BD3 and they are the isosbestic points in the fourth derivative. The length of segment T_{3} 'BK corresponds to the peak height of BD3.

It should be noted that Min3 is the local minimum of the second derivative spectrum of OV3, and Max3 is the local maximum of the fourth derivative spectrum of OV3. A typical local minimum or local maximum indicates that a corresponding component band exists in the vicinity thereof. According to the

illustration of Fig.2, only Min3 is the local minimum of the second derivative spectrum of OV3 and there is no local minimum that corresponds to other component bands BD1 and BD2. On the other hand, according to the illustration of Fig.3, the typical Max3 exists as the local maximum of the fourth derivative spectrum of OV3. Further, although there are other two local maxima, since they are modulated by the side lobe of the dominant peak, it is not clear whether they indicate the existence of the corresponding component bands.

From the description mentioned above, BD3 is the analyzing component in which the local minimum is typically at the second derivative spectrum and in which the local maximum is typically at the fourth derivative and the remaining components OV12 is called "background components". Then, estimating band parameter values is examined based on the algebraic geometry. spectrum where many component bands overlap, generalization is possible by regarding it as the two-component system of the "analyzing" component band and the "background" components. "Two-dimensional derivative plot" refers to plotting the pairs of the n-th and m-th derivatives in the two-dimensional coordinate. It can be abbreviated as "Dn-Dm" plots.

D1-D2 plots are shown in Fig.4, in the two-dimensional representation of the pairs of the first derivative and the second derivative. D3-D4 plots are shown in Fig.5, in two-

dimensional representation of the pairs of the third derivative and the fourth derivative.

Letters and sequential numbers are attached as for the characteristic points of the corresponding component band BD3.

That is, in Figs. 4 and 5, points T3', P31', P32', Q32', and Q33' on OV3 correspond to points T3, P31, P32, Q32, and Q33 on BD3, respectively.

In D1-D2 plots in Fig.4, if the position of T_3' , P_{31}' , or P_{32}' can be estimated, or in D3-D4 plots in Fig.5, if the position of T_3' , Q_{32}' , or Q_{33}' can be estimated, the band center position of BD3 and its bandwidth can be determined by Equation (3) or (4).

In D1-D2 plots in Fig.4, the local minimum Min3 can be a candidate for T3', and the point of intersection of D1-axis, P4, can be a candidate for P32'. However, it should be noted that the X position of Min3 ($X_{min3}=0.3285$) is away from that of point T3' ($X_{T3}=0.4533$), the true value, and the X position of point P4 ($X_{P4}=0.6746$) is far away from that of point P32' ($X_{P32}=0.7963$).

On the other hand, in D3-D4 plots in Fig.5, the local maximum Max3 can be a candidate for T3', and Qd, the point of intersection of D3-axis can be a candidate for Q33'. X position of Max3 ($X_{max3}=0.4180$) is closer to that of point T3'. Further, X position of point Qd ($X_{Qd}=0.6482$) is closer to that of point Q33' ($X_{Q33}=0.7078$), the true value. Concerning the two-dimensional derivative plot, since D1-D2 plots have simpler

shapes than do D3-D4 plots, the explanation goes transferring the characteristic points on D3-D4 plots to those of D1-D2 plots, where the point corresponding to Max3 is denoted Max3' and the inflection point converted by the secondary inflection point Q_d is denoted P_d '.

Iso-wavenumber lines are used for explaining the geometrical relation of the characteristic points on the two-dimensional derivative plot. Iso-wavenumber lines are the straight lines connecting the same wavenumber points between two spectra. In Figs. 4 and 5, since it is complicated to draw the lines over entire range, the iso-wavenumber lines are drawn only in the region of interest. Here, the sequence numbers along the profile represent the wavenumbers.

In Fig. 4, the iso-wavenumber lines passing through point T3' is parallel to D2-axis. Let the point of intersection with OV12 be point Bk, let the point of intersection of the extended iso-wavenumber line and OV3 be point At. The length of line segment T3'Bk corresponds to the peak height of BD3.

On the other hand, the iso-wavenumber lines passing through the inflection points P_{32} ' and P_{31} ', respectively, are parallel to D1-axis. Let the point of intersection of the iso-wavenumber lines passing through point P_{32} ' and OV_{12} be point P_{j} , and let the point of intersection of the extended iso-wavenumber line with respect to P_{32} ' and OV_{12} be point A_p . Let the point of intersection of the iso-wavenumber line passing

through point P31' and OV12 be point P1. The length of line segment P32'Pj equals the length of line segment P31'Pi, which corresponds to a half of the bandwidth between two inflection points of BD3. Let the point of intersection of lines T3'Bk and P32'Pj be point Bj, and let the point of intersection of lines T3'Bk and P32'Pi be point Bi. Further, let the point of intersection of lines T3'Bk and P31'P32' be point Bx.

According to Fig. 4, since points B_k and B_x are above the line which is parallel to D1-axis passing through point P_d and are close to each other, it causes no problem when point B_k is replaced by point B_x . In general, the position of point B_k depends on the shape of background component OV_{12} and it is difficult to find its position by the algebraic geometrical method.

Nevertheless, the permissible region of point B_k can approximately be determined. When the component bands are close to each other, the shape of OV₃ is like that of a single band. At this time, the position of point B_k is below that of point B_k, located in the vicinity of point B_i. Conversely, as the separation between the component bands is large, the position of point B_k moves upward to that of point B_k. Further, when the separation between the component band becomes larger, another local minimum appears on OV₃ and the position of point B_k is located in the vicinity of point B_j which is above point B_k.

On the other hand, as for line segment P32'Pj corresponding to a half of the bandwidth between two inflection points of BD3,

point P_j exists in the left-hand side of point A_p. That is, line segment P₃₂, P_j is shorter than line segment P₃₂, A_p. Likewise, the same analysis can be applied to D₃-D₄ plot in Fig. 5. Based on the geometrical study described above, how to find estimated parameter values of a component band is explained one by one. (Step1)

As can be seen from Fig. 4, the X position of Max3' (or Min3) is the first approximation of band center position Xc for the corresponding component band BD3. Hereafter this point is denoted as eT3. Draw a straight line L1 parallel to D1-axis passing through point eT3. An estimated point eP32, on OV3, for the inflection point P32 of BD3 is placed in the vicinity of the inflection point P4 of OV3. In more detail, the X position of eP32 is at the positive side of that of point P4. Then, an estimated value of the bandwidth of BD3 is calculated by Equation (8). Draw a straight line L2 parallel to D2-axis passing through point eP32. Line L2 intersects line L1 at point B3.

Next, an estimated point eP31, on OV3, for another inflection point of BD3 is placed at the opposite side of point eP32 with respect to point eT3. Both points eP31 and eP32 are equidistant from point eT3 with respect to the X-coordinate or the wavenumber. Line segment eP32 eP31 intersects line L1 at point Bk. From the length of line segment eT3Bj or eT3Bk, an estimated value of the peak height of BD3 is calculated.

Thus, a set of estimated values of band center position

eBC3, bandwidth eBW3, and peak height ePH3 for BD3 can be obtained. In order to obtain the true values or optimal estimated values for BD3, a candidate can be created by finding sets of parameter values on several sequential points as the estimated value of eP32 from the vicinity of point Pd.

It is clear that when an estimated value of band center position eT3 is close to point T3', a better estimated value of a bandwidth can be obtained. Table 1 shows the sets of estimated values of the bandwidth and the peak height for BD3 calculated by using systematic sequential points for eP32 when point eT3 is equal to the true target point T3'. eBW3 is the estimated bandwidth, ePH3A is the peak height obtained by line segment eT3B; , and ePH3B is the peak height obtained by line segment eT3Bx.

Table 1

			•	
Set of estimated value	X coordinate of eP32	eBW ₃	ePH3A	ePH3B
EstBD3a	0.70	0.581	0.357	0.244
EstBD3b	0.71	0.604	0.404	
EstBD3c	0.72	0.628	0.455	
EstBD3d	0.73	0.652	0.509	
EstBD3e	0.74	0.675	0.566	
EstBD3f	0.75	0.699	0.628	
EstBD3g	0.76	0.722	0.693	
EstBD3h	. 0.77	0.746	0.761	
EstBD3i	0.78	0.769	0.833	
EstBD3i	0.79	0.793	0.908	
EstBD3k	0.80	0.816	0.986	
EstBD3l	0.81	0.840	1.07	
EstBD3m	0.82	0.863	1.15	
EstBD3n	0.83	0.887	1.24	1.09

Figure 6 shows the plots of the candidates of estimated values listed in Table 1 with a bandwidth at the Horizontal axis and with a peak height at the Vertical axis. Points a, b, c,....., n on the curve xy (this is called SelLN1) are calculated when peak heights are estimated by the length of line segment eT₃B₃ and sequence a', b', c',....., n' on the curve x'y' (this is called SelLN2) are calculated when peak heights are estimated by the length of line segment eT₃B₃. The point indicated as 'actual' is the true point for BD₃. It is necessary to restrict estimated values from the algebraic geometrical constraint conditions.

According to Fig. 6, the constraint conditions subjected to the estimated values (set of the bandwidth and the peak height) are explained as below. As clearly shown in the spectral profile of Fig.1, since BD3 must be downward of OV3, it must be BD3(X)<OV3(X). Since BD3 must not exceed OV3 at the estimated point of eT3, the band center position of BD3, it must be BD3(eT3)<OV3(eT3). There is the upper limit for the peak height. That is, in Fig. 6, estimated values must lie below the straight line shown as 'OverTop'.

In addition, estimated values must be at the left-hand side of the curved line denoted as 'OverEnv'. When the bandwidth is small, a certain degree of the peak height is permissible, however, when the bandwidth is large, only a relatively small range of the peak height is permissible. Therefore, as shown

in Fig.6, qualitatively, OverEnv is the declined curved line from left to right.

Further, from D1-D2 plots shown in Fig. 4, the constraint conditions subjected to the estimated values can be calculated. From Fig. 4, the position in which the inflection point P32' of BD3 will exist must be above point Pd, the inflection point of OV3. The inflection point for an estimated component band is above point Pd, which means that the bandwidth of the estimated component band is larger than that calculated from point Pd. Correspondingly, this means that the estimated value must be located at the right-hand side of line PDw in Fig. 6. In addition, likewise, since the points Bj and Bx are above point Pd, line segment eT3Bj or eT3Bx ought to be longer than the distance of eT3 from the X-axis. Correspondingly, therefore, in Fig. 6, estimated values must be above line PDh.

Since point Pd' in Fig. 4 which corresponds to inflection point Qd in Fig. 5 has an effect of higher order derivatives, it is clear to be generally closer to point P32'. Therefore, likewise, in Fig. 6, the estimated values must be located above line PDh' and right-hand side of line PDw'. In addition, from point At which was already described, constraint of the peak height is introduced, which means in Fig. 6 that the estimated values are located below straight line OverAt. Therefore, the constraint conditions subjected to a bandwidth and a peak height or permissible range thereof, are within the region of the

hatched polygon bounded by straight lines PDw', PDh', OverEnv, and OverAt.

Which point should be selected as the estimated values from selection line SelLN1 or SelLN2 is explained below. At x' end side of SelLN2, both the bandwidth and the peak height are smaller than the true value. Conversely, since y' end side of SelLN2, both the bandwidth and the peak height are larger than the true value and they exceed the curved line OverEnv. Points j', k', and l' in the vicinity of the middle part of SelLN1 are located close to the true value for BD3. The upper limit of the bandwidth using point Ap (the length of line segment P32'Pj corresponding to a half of the bandwidth of BD3 is smaller than that of line segment P32'Ap) is in the middle of points k' and 1'. The position of the true value for BD3 is around the center of the hatched triangle region shown in Fig. 6 when the degree of overlapping among the component bands is high. And the position of the true value for BD3 is around the curved line OverEnv when the degree of overlapping is low. Around point k' is a good candidate as the estimated values for eBW3 and ePH3.

The procedure of finding estimated values for BD3 was explained as mentioned above, assuming that the estimated value of the band center position is the true one. In general, the estimated value of band center bc3 of component band BD3 is selected as Max3' (Xmax3=0.418).

Then, finding a set of a series of estimated values eBD3,

estimated values for BD3 are selected. At this stage, a set of estimated values for BD3 is obtained (eBC3=0.418, eBW3=0.830, and ePH3=0.780):

Thus far, as for BD3, eBW3, and ePH3, estimated values for three parameters, eBC3, eBW3, ePH3, were obtained. Here, the shape of the component band is assumed to be Gaussian. If the shape of the component band is assumed to be Lorentzian, since the bandwidth is 1.47 times as large as that of Gaussian, the component exceeding OV3 appears. Therefore, the Lorentzian component band is rejected.

After component band BD3 was estimated, a band stripping operation is performed, further estimating a component band. In order to explain this procedure, as an ideal case, algebraic geometrical explanation goes. Figure 7 shows overlaid D1-D2 plots of OV12 (= BD1+BD2) wherein two component band BD1 and BD2 overlapped and BD1. Figure 8 shows D1-D2 plots of OV13 (= BD1+BD3) wherein two component bands BD1 and BD3 overlapped and BD1. Figure 9 shows D1-D2 plots of OV13 and BD3.

As can be seen from Fig.7, since Min2 and Max2' are not close to each other, it is more likely or apparent that overlap between the component bands BD1 and BD2 is strong.

In Figs. 8 and 9, the local maximum Max13 indicates that the typical valley exists between BD3 and BD1. The appearance of the valley arises from the lower degree of overlap compared with that of OV12. In Fig. 8, the curved portion from the origin

O to Min1 via point Pa substantially overlaps with the curved portion of the right half of BD1. Since Min1 and Max1' are not close to each other, around the vertex of BD1, they are affected by overlap of BD2 and/or BD3. In Fig.9, the curved portion from the origin O to Min3 via point Pa substantially superposes on the curved portion of the left half of BD3. Since Min3 and Max3' are close to each other, the band center position of BD3 is in the vicinity thereof.

In Fig. 8, when estimating for BD3, there is no problem when point B_{K} is used for estimating point B_{K} . However, since there is the valley shown in Fig. 9, the curved portion of the left-hand side of BD1 is greatly deformed and since line segment $P_{12}'P_{11}'$ and the perpendicular line to D1-axis passing point T_{1}' do not intersect, point B_{K} exists at a position with line segment $P_{12}'P_{11}'$ extended. In addition, the curved portion from the origin 0 to Min 1 via point P_{a} substantially superposes on the curved portion of the right half of BD1 and point B_{K} is in the vicinity of point B_{K} . Therefore, it is desirable to calculate the peak height from the length of line segment $T_{1}'B_{1}$.

(Step 2)

Now that estimated values were obtained on BD3, BD3 can be expressed mathematically with Equation (6). This is denoted as eBD3. eOV_{12} is found by band stripping eBD3 from OV3. That is, $eOV_{12} = OV_3 - eBD_3$. In Fig.10, D1-D2 plots are shown regarding OV_{12} and eOV_{12} . For comparison, the iso-wavenumber lines are also

drawn. Band parameter values for new component band eBD2 are estimated from eOV12.

By the same procedure taken in Table 1 and Fig. 6, Table 2 and Fig.11 are prepared. Estimated values for BD2 are selected in the vicinity of point h' in Fig.11. That is, eBC2 = -0.08, eBW2 = 1.11, ePH2 = 1.06. In this case, the true value for BD2 indicated as 'actual' is not within the hatched triangle. This is due to the poorly estimated parameter values for eBC3. However, an iterative operation described later can improve band parameter values for eBC3.

Table 2

10010 2							
Set of estimated value	X coordinate of eP22	eBW ₂	ePH2A	ePH2B			
	0.360		0.982	0.866			
EstBD2a	0.365						
EstBD2b							
EstBD2c	0.370		1.09				
EstBD2d	0.375						
EstBD2e	0.380						
EstBD2f	0.385			1			
EstBD2g	0.390	1					
EstBD2h	0.395						
EstBD2i	0.400						
EstBD2j	0.40		1	-			
EstBD2k	0.410	1.15					
EstBD2l	0.41	5 1.1'					
EstBD2m	0.420	0 1.18					
EstBD2n	0.42	5 1.19	$\frac{1.4}{}$	$7 \qquad 1.31$			

(Step3)

eOV₁₃ is found by band stripping eBD₂ from OV₃. D1-D2 plots regarding eOV₁₃ are shown in Fig.12. As is clear from Fig.12, since two local minima appear, it is found that there are at least three component bands within OV₃ and the band center position could be estimated. Here, local minima Min1 and Min 3 indicate the existence of corresponding component bands BD₁ and BD₃, respectively.

When the positions of Max 1' and Max 3' corresponding to Min 1 (Xmin1=-0.8257) and Min 3 (Xmin3=0.4276), respectively, are calculated, Xmax1=-0.7757 and Xmax3=0.4403. Min 3 and Max 3' found here are closer to the true value T3' compared to Min 3 and Max 3' in Fig.4 or 5. This is due to band stripping effect, which has reduced overlapping effect between component bands.

Therefore, eBC3 in Step 1 is replaced by Xmax3 just obtained, and a set of eBD3 and its constraint conditions are recalculated in the same manner as in Step 1. At the same time, constraint conditions are also calculated from Fig.12. The set of eBD3 obtained by this and the constraint conditions are shown in Table 3 and Fig.13. According to the results, constraint conditions subjected to them are the narrower permissible regions. The intermediate point of points i' and j' on Se1LN2 is selected as a new estimated point. That is, eBC3 = 0.44, eBW3 = 0.81, and ePH3 = 0.78.

Table3

Set of estimated value	X coordinate of eP32	eBW_3	ePH3A	ePH3B
EstBD3a	0.70	0.612	0.409	0.284
EstBD3b	0.71	0.636	0.46	0.326
EstBD3c	0.72	0.659	0.515	0.372
EstBD3d	0.73	0.683	0.574	0.422
EstBD3e	0.74	0.706	0.636	0.476
EstBD3f	0.75	0.730	0.702	0.535
$\mathbf{EstBD3g}$	0.76	0.753	0.772	0.598
$\mathbf{EstBD3h}$	0.77	0.777	0.846	0.666
$\mathbf{EstBD3i}$	0.78	0.801	0.923	0.739
EstBD3j	0.79	0.824	1.0	0.816
EstBD3k	0.80	0.848	1.09	0.899
$\mathbf{EstBD31}$	0.81	0.871	1.17	0.986
EstBD3m	0.82	0.895	1.26	1.08
$\mathbf{EstBD3n}$	0.83	0.918	1.36	1.18

(Step4)

When the band parameter values for BD2 are estimated in the same procedure as in the Step 2, eBC2 = -0.03, eBW2 = 1.04, and ePH2 = 1.01.

When compared with the result of the Step 2, the suitability is improved.

(Step5)

Further, by iterating the same procedure as in the Step3, a new set of estimated values for BD3 is obtained. That is, eBC3 = 0.449, eBW3 = 0.814, and ePH3 = 0.800.

(Step6)

Further, band parameter values for BD2 are estimated and eBC2=-0.02, eBW2=1.04, and ePH2=0.967. Judging that estimated values are no longer improved with the iterative operation, the operation is hereby suspended.

(Step7)

Finally, band parameter values for BD1 are estimated. This can be found by the geometry illustrated in Fig.9. That is, eBC1 = -0.642, eBW1 = 1.15, and ePH1 = 0.512. In addition, when the suitability of estimated parameter values for BD2 and BD3 is good, by D1-D2 plots where eBD1 = OV3 - eBD2 - eBD3, the band parameter values for eBD1 can also be estimated. In Fig.14, D1-D2 plots of eBD1 and ePH1 = 0.512 and ePH1 = 0.512. In addition, when the suitability of estimated parameter values for eBD2 and ePH1 = 0.512. In addition, when the suitability of estimated parameter values for eBD1 can also be estimated. In Fig.14, D1-D2 plots of eBD1 and ePH1 = 0.512 and ePH1 = 0.512. In addition, when the suitability of estimated parameter values for eBD1 can also be estimated. In Fig.14, D1-D2 plots of eBD1 and ePH1 = 0.512.

These results show that estimated values of eBD2 or eBD3

are not good. Although the existence of the fourth component band cannot be denied, it cannot be judged from the estimated values obtained so far. Therefore, complementary matching is conducted assuming that there are three component bands.

For confirmation, the estimated values at this stage are as follows:

Estimated component band eBD1: eBC1 = -0.642

eBW1 = 1.15

 $ePH_1 = 0.512$

Estimated component band eBD2: eBC2 = 0.002

 $eBW_2 = 1.01$

 $ePH_2 = 0.967$

Estimated component band eBD3: eBC3 = 0.449

 $eBW_3 = 0.814$

 $ePH_3 = 0.800$

(Complementary Matching)

The suitability of the component bands estimated at the present stage is examined. In Fig.15, eBD1 eBD2 eBD3 and eOV3 are shown together with OV3. In Fig. 16, D1-D2 plots of eOV3 and OV3 are shown. In the figures, the iso-wavenumber lines between OV3 and eOV3 were also drawn and the profiles of eOV3 and OV3 are not coincident. However, since it is hard to examine from Fig.15 or 16 which component band has good or poor suitability for an

estimation, the improvement of band parameter values should be performed and evaluated according to other criteria.

Therefore, with a complementary estimated component band, the improvement of band parameter, values is achieved. Here, a complementary estimated component band is the component band subtracting all the other component bands except only one component band between estimated component bands from the spectrum. That is, the complementary estimated component band CBD3 with respect to BD3 is represented as CBD3 =OV3-eBD1-eBD2. If estimated values of all the band parameters are coincident with the true values, eBD3 and cBD3 are also coincident. Likewise, the complementary estimated component band cBD2 or cBD1 can be calculated.

Figure 17 shows D1-D2 plots of eBD3 and cBD3. Likewise, Figs.18 and 19 show D1-D2 plots of eBD2 and cBD2, and eBD1 and cBD1, respectively. In Fig. 17, since Min3 (Xmin3=0.4363), the characteristic point of cBD3, is close to Max3' (Xmax3=0.4465), the band center position may be estimated at the corresponding local maximum or minimum value of eBD3. The right-hand side of the plot is smaller compared with eBD3. This may be because eBD2 or eBD3 is estimated smaller than the true value.

Next, in Fig.18, eBD2 is examined. Since Min2 (X_{min2} =-0.0195), the characteristic point of cBD2, is close to Max2' (X_{max2} =-0.0152), the band center position of BD2 may be estimated at the corresponding local maximum or minimum value of eBD2.

The plot of a single band is heart-shaped since the peak height $\ensuremath{\mathsf{ePH}}\xspace_2$ is estimated smaller than the true value.

Further, in Fig.19, eBD1 is examined. Min1 (Xmin1=-0.6390), the characteristic point of cBD1, and Max1' (Xmax1=-0.7038) are not close to each other. In addition, since the degree of the symmetry of the shape of cBD1 is not good, the estimated values for the band parameters are not good.

Now that suitability of an estimation of each component band was made clear, suitability is enhanced by adjusting each band parameter value. As the criteria for suitability of an evaluation value, SumLS, the total sum of the distances of the iso-wavenumber lines between OV3 and eOV3 on D1-D2 plots is provided and by adjusting each parameter value so as to make the evaluation value small, suitability is enhanced.

As examined from the profiles of Figs.17 to 19, first, parameter values for eBD1 are adjusted. Adjustment is performed in the order of eBD1, eBW1, and ePH1. New eBC1 is determined as the estimated value when SumLS is the minimum by changing it in the vicinity of the current eBC1. When SumLS is calculated and eBC1 is adjusted regarding the total range of X ($-2 \le X \le 2$), eBC1=-0.576. When SumLS is calculated and eBC1 is adjusted within the limited range of the inflection points P11 to P12, eBC1=-0.594. Further, when SumLS is calculated and eBC1 is adjusted within the limited range of the secondary inflection points Q12 to Q13, eBC1=-0.600. Since the true value of BC1 is

-0.5978, at the early stage of the optimization of band center position, that is, at the stage where suitability of the estimation is poor, it is better to estimate the band center position limiting to the vicinity of a corresponding local maximum or minimum to calculate SumLS and adjust the parameters.

Likewise, as for estimating eBW1, adjustment is performed. As for estimating ePH1, it is better to find such ePH1 as making SumLS minimum regarding the entire ranges of X.

The same kind of operation is conducted on eBD2 and eBD3 as well. Figures 20 to 22 show D1-D2 plots of the complementary estimated component band after iterating a series of the parameter values adjustment three times. Compared Figs. 17 to 19, suitability of the band parameter values is improved.

The optimization of all the band parameter values cannot be simultaneously achieved when the estimated value of each band parameter values is adjusted alone. The optimization of the estimated values for eBD1 are so adjusted as to enhance the degree of coincidence between eBD1 and cBD1 as well as to improve the symmetry of cBD2 which is the adjacent complementary estimated component band in Fig.18.

Here, the criteria of symmetry are so defined that two inflection points are symmetrical to the Y-axis. That is, for example, the parameter values are so adjusted that the length of the line segment OP11 is equal to that of the line segment OP12.

For example, in adjusting ePH1, ePH11 where SumLS is the minimum (ePH11 = 0.646) is found. Next, ePH11 is found where the length of line segment OP11 is equal to that of line segment OP12. Then its mean value (ePH11+ ePH11)/2 is selected as an optimum estimated value. The reason for selecting the mean value is that the symmetry of cBD2 is affected from the band of both sides. By such iterated operations, ePH11 and ePH11 become coincident.

In adjusting the band center position eBC1, the above operation is not always required since the good estimated value is obtained for eBC1 where SumLS has the minimum value. Likewise, the improvement of the coincidence between eBD2 and cBD2 and in the symmetry of cBD2 is achieved. The results are shown in Figs. 23 to 25. Finally, the good results were obtained as follows:

Estimated component band eBD1: eBC1 = -0.597

 $eBW_1 = 1.094$

 $ePH_1 = 0.648$

Estimated component band eBD2: eBC2 = 0.004

 $eBW_2 = 0.952$

 $ePH_2 = 1.070$

Estimated component band eBD3: eBC3 = 0.456

 $eBW_3 = 0.794$

 $ePH_3 = 0.800$

Finally, the examination of the existence of the hidden component bands or the evaluation of the residual component rBD

is performed. rBD is represented as rBD = OV3-eBD1-eBD2-eBD3. Virtual component band vBD whose parameter values are already known is introduced and D1-D2 plots of the data with rBD, remaining component bands, and vBD added are evaluated. Since the derivative plot of vBD is already known, it can be evaluated by the shape of the overlapping residual component. In addition, an evaluation of a complementary estimated component band is also made. Thus, when a hidden component band can be estimated, it is a good way to return to the first step, finding the estimated value of parameter values for a new component band from constraint conditions, thereby improving the parameter values of the said component band by the similar method.

The estimation method of the present invention was described above by using the simulation data. In estimating actually measured data, it is necessary to differentiate digitally in order to obtain derivatives plots. Therefore, in the case where the band to be measured is sharp, it is necessary to measure with the small data interval for measurement.

Particularly, in the present invention, as for the analyzed object, what matters is a method of analyzing the obtained data and in order to obtain the data, the conventional spectrophotometer can be used as it is thereby requiring no new spectrophotometer. The component bands can be estimated from the spectral data of the analyzed object by outputting spectral information, thereafter putting into a data station or a computer

with programs developed based on the proposed method. These programs can be installed into the spectrophotometer.

(Effect of the Invention)

When the procedure of the spectral analysis method of the present invention is used, several component bands can be easily estimated as for the analyzed object having a spectral profile which contains several component bands.

Summary on the procedure of the spectral analysis described above is as follows:

- (1) The band center position of corresponding component band is determined noting the typical local minimum, and/or local maximum of the two-dimensional derivative plot (including D1-D2 plots) of the spectra of the analyzed object.
- (2) The candidates for the bandwidth values are determined by selecting candidates of several points in the vicinity of zero-crossing points of the second derivatives, estimating the bandwidth of the corresponding component band from the candidates of inflection points, and estimating the peak height of the corresponding component band from the algebraic geometrical condition of two-dimensional derivative plot. Further, band parameter values are imposed by the constraint conditions and the estimated value is determined.
- (3) The band parameter values are estimated by finding the component bands in order by band stripping.
 - (4) The estimated band parameter values are optimized and

improved by using the complementary matching method and considering the overlapping effects among component bands.

- (5) The band parameter values for component bands are determined among best fitting band shape since the profile of each component band must be line symmetry when each component band is extracted.
- (6) Suitability of the band shape and existence of hidden bands are examined by observing profile of each component band after optimization of the band parameter values.

Description of the preferred embodiment described herein is illustrative and not restrictive, the scope of the invention being indicated by the appended claims and all variations which come within the meaning of the claims are intended to be embraced therein.